



Report No. 4

Hydraulics of Single Span Arch Bridge Constrictions

by

P. F. Biery
Research Engineer, Johns Manville, Inc., Manville, N.J.
formerly Research Assistant, Furdue University

and

J. W. Delleur Associate Professor of Hydraulic Engineering

> State Mighway Department of Indiana in Cooperation with U.S. Department of Commerce Bureau of Public Roads

Joint Highway Research Project Project No. G-36-62B File No. 9-8-2

Purdue University
School of Civil Engineering
Hydraulic Laboratory

May, 1961

Digitized by the Internet Archive in 2011 with funding from LYRASIS members and Sloan Foundation; Indiana Department of Transportation
http://www.archive.org/details/hydraulicsofsing00bier

HYDRAULICS OF SINGLE SPIN ARCH BRIDGE CONSTRUCTION² by P. F. Biory², AM.ASCE and J. W. Dellour³, H.ASCE

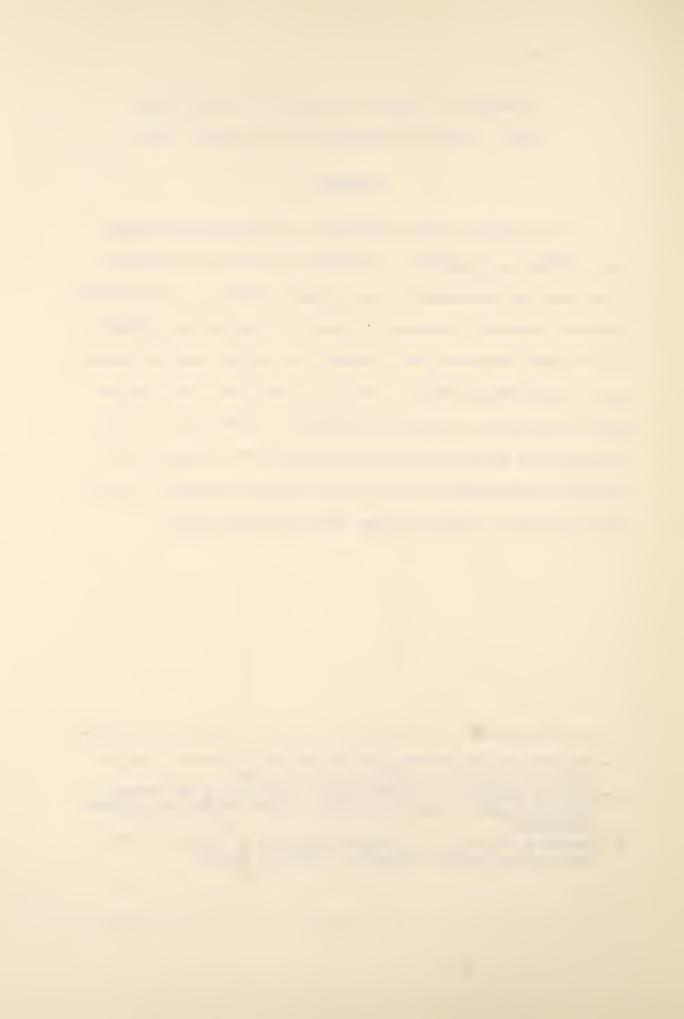
Sympsis

constrictions are presented. All tests were win for the condition of no skew, no eccentricity and no entrance rounding. A generalized backwater superclavation in terms of the bridge span, the stream width and the Frouds number of the approaching flow. The equation holds for geometries other than semicircular constrictions. Design procedures for indirect discharge measurement, for determination of backwater superclavation, and for determination of required waterway area are given. A model-prototype comparison is discussed.

^{1 -} Presented at the national ASGE convention, Hydraulic Division, Hydraulic Structures Session, October 16, 1960

^{2 -} Research Engineer, Johns Manville, Inc., Manville, New Jersey, formerly Research Assistant, School of Civil Engineering, Purdue University

^{3 -} Associate Professor of Hydraulic Engineering, School of Civil Engineering, Purdus University, Lafayette, Indiana



INTEODUCTION

In recent years, the problem of protecting the flood plains from flood damage has become increasingly important. In order to eliminate or minimize any additional flood effects, the highway engineer must be able to predict the influence of a new highway bridge upon viver stages during high flood flows. It is generally recognized that the introduction of a bridge crossing interferes with the natural flow of the stream and results in a rice in stage upstream and an increase in velocity through the bridge. It is the highway engineer's responsibility to provide the minimum span length for structural and economic reasons, and yot to allow a large enough water area to keep the rice in backwater within tolerable limits. Without the necessary information to make an intelligent estimate of the maximum backwater, overdesign or underdesign results in making either the cost of the bridge prohibitive or the rick of flood damage excessive.

In the past, studies by the U. S. Geological Survey and the Bureau of Public Roads pertaining to the backenter effects caused by bridge constrictions have considered shapes of spenings such as those produced by straight dark bridges. However, very little has been done in the way of making a systematic study of the hydraulies of river flow under the various shapes of arch bridges. The arch is unique in that the surface width of the water surface within the barrel of the arch decreases with a corresponding increase in stage.

A project was initiated in the Hydraulies Laboratory at Purdus University to study the hydraulies of stream flow under arch bridges. It is sponsored by the Indiana State Highway Department in cooperation with



the U.S. Bureau of Public Roads. The purpose of this research is to study the hydraulics of arch bridge constructions and to provide a method for computing the backwater upstream of the bridge.

The carliest systematic laboratory investigation of flow through contractions in open channels was performed by E. W. Lans. 18 He related the discharge and the water surface elevation through the contraction by means of empirical discharge coefficients, and indicated that there may exist some relationship between these coefficients and the ratio of the maximum backwater depth produced by the contraction to the normal depth of flow without the contraction. This ratio is referred to as the backwater ratio.

In 1955, Kinsvater and Carter² presented a practical solution to the discharge quation by an extensive experimental investigation. By applying correction terms for various geometric conditions to a standard discharge coefficient, the method can be applied to a wide variety of boundary conditions. A detailed description of the internal and external flow characteristics was given.

In the same year, H. J. Tracy and R. W. Carter presented a companion paper to the one by Kindsvater and Carter. In it they gave a method of computing the nominal backwater due to open channel constrictions. The practical solution was based upon empirical discharge coefficients and a laboratory investigation of the influence of channel resughness, channel shape, and constriction geometry. Their study was limited to single span, dock type constrictions and to steady tranquil flow. C. F. Izzard, in his discussion of this paper, pointed out that the backwater ratio expressed as y_1/y_n (see Figure 1) is a function of the normal depth

^{*} Superscripts refer to references in the bibliography.



Fronds number at the constricted section. Also, he questioned the use of the backwater ratio in terms of hy /Ah when the head loss between the section of maximum backwater and the vena contracta is large compared to the approach velocity head.

In 1953, some of the combined efforts of Kindsvater, Carter, and Tracy were organized into a U. S. Geological Survey Circular. It presented a method for determining peak discharge at abrupt contractions. The discharge estimate was to be made from a survey of high vater marks and channel characteristics. Although the method applies well to deck type bridges, there is no direct application for using the method when an arch bridge is used to make an indirect measurement.

In Outober 1957, the Colorado State University in cooperation with the U. S. Bureau of Public Roads published a bulletin by H. K. Idu⁶, J. N. Bradley and E. J. Plate entitled "Backwater Effects of Piers and Abutments". A rigorous and extensive invertigation of the backwater effects of piers and abutments has been given. The paper includes a complete analysis of the energy losses through the constriction. An approximate simple method of analysis is provided for the highway engineer to use. The general principle of the method is the conservation of energy. A number of graphs based upon laboratory data were developed for datermining the maximum tackwater and the differential level of water surface elevations across the embankment. Much of the work done at Colorado has been used as a comparison to the present research.

Based upon the model tests conducted at Colorado State University,

J. N. Bradley compiled a report entitled "Hydraulics of Bridge Waterways".

The publication was completed in August 1960 and is the first in a series of reports on the hydraulic design of highway drainage structures. This



particular report, within limitations, is intended to provide a means of computing the effect of a given bridge upon the flow in a stream.

H. R. Vallentine reports on tests performed to study the characteristics of flow in a rectangular channel with symmetrically placed sharp edged constriction plates placed normal to the flow. The flow is related to the upstream depth by means of a weir type discharge equation. The experimental coefficients were found to depend upon the geometry of the constriction and the Froude number of the unconstricted flow. The conditions which produce an increase in the upstream depth were investigated and the extent of the increase evaluated.

Some recent work done at lehigh University tells about the effects of placing spur dikes on the upstream side of a bridge contraction. These dikes are designed to increase the hydraulic efficiency of the bridge crossing by lowering the backwater curve and reducing the scour undermeath the bridge. This particular report presents a good qualitative description of the flow patterns through the bridge embankments.

A preliminary investigation including some model testing of samicircular arch constrictions was done at Purdum University by Owen, Sooky,
Humain and Delleum 10 in 1958 and 1959. The backsater superelevation was
related to the Freude number of the approaching flow and to the ratio of the
arch span to the stream width. The present paper is an outgrowth of this
preliminary study.



THEORETICAL ANALYSIS

Dimensional Considerations

Figure 1 shows a definition sketch of the effects of a charmel constriction on the water surface profile. Section view B illustrates the type of centerlins profile obtained with a mild slope channel. This is the most generally occurring situation that appears in actual practice. In the ingure y_0 or y_0 is the normal depth of the unobstructed channel, y_1 is the depth at the point of maximum backwater slevation, y_2 is the depth at the section of minimum jet area or the vena contracts, y_3 is the minimum water depth of the regain curve, and y_0 is at a point sufficiently downstream from the contraction where the flow returns to the normal depth.

A dimensional analysis was made for the purpose of guidance and interpretation of the testing program. In this manner the basic variables can be grouped into dimensionless quantities and their relationships investigated. In the problem at hand, it is desired to determine the maximum water depth upstream of the constriction. It is assumed that the variables which govern the backwater superelevation may be grouped into three catagories as follows: the fluid properties, the kinematic and dynamic variables, and the dimensional defining the boundary geometry. Due to the two dimensional character of the constriction, the latter is expressed in terms of flow areas rather than the usual limear dimensions.

The variables are: (see Figure 1)

- a.) Fluid Properties
 - p, the kinemetic viscosity of the fluid
 - p, density of the fluid
- b.) Kinematic and Dynamic Flow Variables
 - g, acceleration of gravity



- TI, TRITED TEXAS COLUMN TO SE Al tin monstriulina.
- The north cepth of flor in the opproach claimed
- Vas to relaity of floors no not depth
- n limiting a roughness to disciplify of the approach changes
- an, the limit of the series of the constriction of the constrictio
- The Properties of the Contributed Geometry

 11: the south Anna Copie flor are at the chien l

 10: the arm lough flor are at the up three feet of

 the architectualism

Among the stone that of varientle,

The distribute the conflictuates within a physical coolem including a quantitie of the arranged arts in a distribute at the arranged arts in a distribute at the arranged arts in a mass, longth and time against a function the new or simplification to parameters are as follows:

Inverting the flow on page care

11 7 = 3/72 7 = 13/1/ 2/1/ 2/1/ 2/1/2 = 1/2/2 = 1/2/2 = 1/2/2 = 1/2/2 = -3/2/2 = 1/2/2 = -3/2/2 = 1/2/

In square of the normal depth Troude number. It is well known that gravity forces are predominant in open that well flow therman viscous forms play a community role. The Populois number $T_{\rm eff}$ is the theregorised in the determination of y/y_n . Furthermore, by assuming the manufacture of the water surface upstream is not reterially affected by the shape of the water surface domastream, the term (h/y_n) can



The second of th

die de la company de la compan

$$x = w_1 + \frac{1}{2} v_1 V_{13} V_{13} + \frac{1}{2} v_2 V_{13}$$

$$--(7)$$

The state of the s

Fig. (1) below the upth of a semicircular serious of a semicircular

$$I_{n2} = \left(\frac{2}{2} + \frac{3}{2} + \frac{$$

The second of the bold since and spring the second of the second spring.



The area of the arch segment GNF is

$$A_{52} = \begin{cases} 2 & 3^2 = 3^2 & 3^2 & 3 \end{cases}$$
 $2 / 3^2 = 3^2 & 3^2 & 3 \end{cases}$...(9)

ard the corresponding chang l or ning ratio is

$$H' = A_{n2}/A_{n2} = D\sqrt{E^2 - D^2} + \frac{2}{2} \sin^{-1}D/E = \frac{d\sqrt{r^2 - d^2} + r^2 \sin^{-1}d/E}{By_n}$$

$$By_n$$

$$(10)$$

The change opening ratio 11 can be expressed in terms of three dimensionless ratios; the ratio of spen to channel whith M = b/B, the ratio of depth of the arch center below the stranged to the arch radius q = d/r and tos ratio of normal depth to arch radius = 70/r The channel opening ratio of equation (10) may thus be expressed as:

where

$$c_{M} = 1/2 \left[\frac{\sqrt{1 - (\eta + 5)^{2}} + (\eta + 5)^{5/N^{-1}}(\eta + 5)}{\frac{5}{\eta + 5}} - \frac{\sqrt{1 - \eta^{2}}}{\frac{5}{\eta}} + \frac{1}{\sqrt{1 - \eta^{2}}} \right] - (12)$$
with
$$\eta = d/s$$

and

In the form of equation (11) the value of M = b/B is adjusted for the particular arch by an amount equivalent to CM such that Mo is the ratio of And to Anto In the more general case, the values of 3 and my can take on numbers within certain limits, before the normal depth will submerge the crown of the arch. The limits are as follows:

For
$$y_n/p = 0/p y_n/p \leq (p-1/p)$$
 --- (13)

OF

When 1 0, the case of a semicircular arch with the center of curvature at the springline exists. When 1 = 1, the contraction reduces to two parallel abutments.

The values of C_M have been calculated for several values of 3 and mand are given in the graph of Figure 3. The submergence limit represents the upper limits of both 3 and 7. The segment arch which is a constant radius arch with its center of curvature below the springline of the arch (i.e. 7>0) can be used as an arch in its own right or as an approximation to an elliptical or a multiple radius arch. The value of M' for the elliptic and multiple radius arch could be determined directly from equation (7). However, they have not been worked out in the present research. If equation (11) were applied to vertical abutment bridge piers as idedized in Figure 2a, the value of C_M would become unity.

An approximate form of the equation for the discharge through a two dimensional semicircular arch constriction in a rectangular channel may be expressed in terms of an infinite series of powers of the yyr. With reference to figure 1, the Bernoulli theorem gives:

$$Q = \int V dA = \int_{A} C \sqrt{58(\lambda J - \mu)} \times 5\sqrt{25 - \mu_5} d\mu$$
 --(17)

Expanding equation (14) into a series and integrating term by term and making use of the fact that 2r = b:

$$Q = C_{\rm d}\sqrt{2g} \, 17/24 \, y_1^{3/2} \, b \left[1 - 0.1294 (y_1/r)^2 - 0.0177 (y_1/r)^4 \right] - (15)$$
This may be written as

$$Q = C_{y1}^{3/2}b$$
 T --- (16)

where
$$C = C_{ij} \, 17/24 \sqrt{28}$$



and
$$2 = [(1 - 0.129)(y_1/x)^2 - 0.0177(y_1/x)^4 - -)]$$
 ---(18)

The alsoharge in a rectangular approach channel may also be expressed by

$$Q = V_n A_n = F_n \sqrt{\epsilon} B y_n^{3/p}$$
where
$$F_n = V_n / \sqrt{\epsilon} y_n$$

is the Froude number of the undisturbed normal depth flow. Equating (15) and solving for the discharge coefficient

$$C_{d} = (12\sqrt{2} \text{ F}_{\pi}/17 \text{ N} \text{ T})(y_{\pi}/\overline{y})^{3/2}$$
 ---(20)

Typical values of the coefficient of discharge Cd are shown in figure 8 which shows the results of the two dimensional semicircular arch tests in the rough rectnagular channel. It is interesting to note the limiting conditions of the discharge coefficient as M¹ goes from zero to one. For a two dimensional ideal orifice, Streeter¹² shows that the application of the theory of free streamlines leads to an ideal discharge coefficient of

The coefficient of discharge curves of figure 8 converge to 0.611 showing that this is a limiting value of $C_{\bf d}$ as M^{\dagger} approaches zero.

When M* is equal to unity, $C_{\rm M}$ = 1 and b/B = 1. Therefore, b = B and there is no contraction at all. If there is no contraction, then $y_1/y_{\rm m}=1$ and T=1. Also $12\sqrt{2}/17=0.9981$ which is approximately unity. Therefore equation (20) becomes

Therefore as the opening ratio tends to unity, the discharge coefficient tends to the Frouds number of the undisturbed flow.



The Backwater Ratio Equation

The backwater ratio is defined as the ratio of the maximum centerline water depth to the normal depth of flow. Since $M = M^2/C$ equation (20) may be rearranged such that the backwater ratio becomes

$$y_1/y_n = (12\sqrt{2} F_n / 17 C_d M T)^{3/3}$$
(23)

It has been observed that the equations derived by several different investigators for the beckwater ratio produced by various constriction geometries seem to have a basic similarity. As an example, equation (23) in the present text for y_1/y_1 appears to be a function of $(F/H^2)^{3/3}$.

$$y_1/y_0 = g_1(P_0/M^0)^{3/3}$$
 (24)

An equation for the backwater rathe given by Valentine 6 for lateral constriction plates is

$$y_1 / y_2 = (g F_2 / C H)^{2/3} = c_2 (F_2 / H^2)^{2/3}$$
 --(25)

Also lin⁶ presents an empirical formula for a two dimensional vertical board model

$$(h_1^2/h_1)^3 = h_0 h_0^2 = \frac{2}{3} (\frac{1}{3} - \frac{2}{3} (2.5 - M)) - 1$$
 -- (26)

Considering only the leading term 1/M2 of the quantity in brackets, equation (26) becomes

$$h_1^*/h_0 = S_3 (F_0/M^0)^{2/3}$$
 —(27)

Therefore it appears possible that with the proper interpretation of the variables, namely M⁰ and F_N, the results of tests performed on different geometric shapes of bridge openings may produce the same results. For instance, a vertical abutment deck type bridge may physically appear completely different from a semicircular arch bridge. However, for hydraulic considerations, if they have the same opening ratio M⁰, they may produce the same backwater ratio. The limitations of the assumption must recessarily lie in the fact that both bridges must have the same



that this concept applies equally as well to multiple span bridges. An attempt has been made to compare the two dimensional samicircular test results the eagment data, and the Vertical Board (VB) data as given by Liu. The results of this comparison in Figure 14 have substantiated the assumption of the similarity between the functions g_1, g_2 and g_3 .

EXPERIMENTAL EQUIPMENT

Small Flure and Modela

For the purpose of preliminary testing, a small variable slope flume 6" wide and 12" long was used. The channel sides and bottom were constructed of lucite and carefully aligned by means of adjusting screws. The slope of the flume was controlled by a hand operated scissor jack at the lower end of the flume. An aluminum X-beam mounted horizontally above the flume served as a track for the mechanical and electric point gages used in obtaining the water surface measurements. The flow was metered by a linch orifice plate in a 2 inch supply line. Two and three dimensional models were tested with both smooth and rough boundaries. For the rough boundary tests, the bottom and the walls were lined with copper wire mesh of 16 meshes per inch.

The two dimensional semicircular models were constructed with diameters of 3, 4, and 5 inches. The material used was brass. The edges were machined to 1/32 of an inch and then beveled to a 45 degree angle. The two dimensional segment models were of the same type of construction as the semicircular models and had a value of $\eta = d/r$ equal to 0.5 (see Figure 2b). The three dimensional semicircular models for the small flume were made of clear lucite. The length for all three dimensional models was 24 inches. The testing of segment arches was limited to the small flume only.



Large Flyns and Mcdels

The majority of the tests reported here were performed in a larger 2 feet by 5 foot by 64 foot all steel tilting flums. The slope was controlled by six screw jacks driven by a common motor and gear reducer. The motor was operated by a raise, lower and stop switch. A revolution counter was attached at one end of the drive shaft and the actual slope of the flume bed was related to the number of revolutions and tenths of revolutions of the shaft. In this manner a change of slope with an accuracy of 10.0000025 fcet/foot was easily accomplished in a matter of minutes. An 8 foot by 10 foot head box was equipped with an elliptical transition to provide a smooth change as the water flowed into the flower. The head box also contained several screens and one larger stone baffle. A skimming board which floated on the water surface prevented the propagation of surface waves in the flume. At the discharge end of the flume an adjustable sharp created rectangular wair made of lucite was installed. A catchment box was made to eliminate any splash. The box discharged directly to the sump. The water was taken from a large regirculatory sump. One 2000 GFM pump and one 300 GFM pump fed the head box. The actual inflow was metered by two venturis. The layout of the flume and the water supply system is shown in Figure 4

An aluminum instrument carriage was mounted on adjustable steinlass steel guide rails running the length of the flume. It was installed
in such a manner that the flume bottom could be used as a reference plans.
On the rack were mounted an electric point gage and a 1/4 inch Prandtl
tube. The staff of the point gage was marked in millimeters and was
equipped with a vernier which read to a tenth of a millimeter. The
Prandtl tube was the type used normally for air. It was connected to an
inverted U manometer which had a fluid of specific gravity 0.610. In
addition a 50-tube piezometer stand was installed to obtain rapid



points along the centerline and 1 ft. and 2 ft. right and left of the centerline were hooked up to the piezomete: blak. The bank was constructed so that it could be tilted to a 4,7 degree angle and was illuminated from the incide.

Sixteen models were used in the testing program. They were designed for specific values of b/B and L/b, where L is the length of the model measured in the direction of the flow. For a relative length ratio of L/b = 0, four models were made, one for each of the following values of $M = b/B_0$ M = 0.3, 0.5, 0.7, and 0.9. They were constructed with <math>1/2inch marine plywood and faced with 22 gauge falvanized sheet metal. The three dimensional models were built with M values of 0.3, 0.5, 0.7, and 0.9. In each M group two modals were constructed with L/b = 0.25 and one model with L/L = 0.5. The main construction was 1/2 inch marine plywood. The barrel was formed with galvanized sheet metal and one side of one of the L/b = 0.25 models was faced with lucite. Figure 5 illustrates the three dimensional bridge models. Shown are the four models with L/b = 0.25 and M = 0.3, 0.5, 0.7, and 0.7. With this combination of models it was posable to test each of the sponings M = 0.3, 0.5, 0.7, and 0.9 for relative lengths L/b of 0, 0,25, 0,50, 0,75, and 1,00, All of the models tested in the large flume were either two or three dimensional semicircular models. The testing section was located between 20 and 50 feet from the entrance where it was possible to maintain uniform flow. In all cases the regain curve between sections 3 and & (Figure 1) was within the test section. In the great majority of the cases the boundary layer was fully developed within the first 20 feet of the flume, and fully developed uniform flow existed in the test sections

The citual testing programma in the large flues we run under two differ not been are roughness on forms. The first congruence which will be



referred to as the smooth boundary consisted of the steel flume walls being fini had with an epoxy rasin paint.

Manning on for smooth boundaries had an average value of 0.0110. The range of n was from 0,009 to 0.0130 for discharges and Froude numbers from 1 cfs to 4 cfs and 0.05 to 1.00 respectively.

For the rough boundarie, the following roughness pattern was selected. Along the bottom of the flums, two layers of 1/4 inch aluminum rods were placed; a botton layer of longitudinal bars placed 12 inches on center, and a top lay 1 of tra sverse bare 6 inches on center. Along the sidewalls one layer of vertical bars 6 inches on center was placed 1/4 inch from the wall. The bettom layors of bars were tied together with wire. The vertical bars were tied at the botton to the transverse bars and clamped to the well above the free surface. The value of Marning's n for the rough boundaries ranged from 0.022 to 0.025 for discharges from 1 to 3 ofs and elepse from 0.000010 to 0.00450. The average value of n of 72 uniform flow tests was 0.0238.

Te sta

Seventy tosts were run in the large flums with smooth boundaries covering a range of discharges from 1 to 2.5 cfs and a charmel width ratio M varying from 0.3 to 0.9. One hundred and sixty eight tests were made in the large flume with rough boundaries for the conditions summarized in the table below, where the X's indicate the selected normal depth conditions for each of which the following values of M and L/bs

For M = b/B = 0.3. 0.5. 0.7. 0.9

and L/h = 0.0. 0.5. 1.0

	ena L/C	3 0.00 00	79 20 U				And the last of th
Flow Rate 1. cfs 2 cf- 3 cfs	X	0.15.0.20	0.25 0 30	o Number	(0.1) 10.5	0 0.60 0.70 Z	0.60 0.90



Also with rough boundaries additional tests were made to establish that the expansion of the flow downstream from the minimum depth (profile between points 3 and 4 of Figure b) was complete and within the limits of the test section. A detailed surface topography was measured for Q = 1 cfs, slope = 0.00584, M = 0.5 and L/b = 0. Sufficient velocity profiles were taken at these conditions to plot isovel diagrams for the sections of uniform depth, maximum depth, vena contracta and the minimum depth. The isovel diagrams were also obtained for uniform flow corresponding to the following conditions:

Q = 1 cfs; slope = 0.004080

Q = 2 cfs; slope = 0.000131

The particular measurements that were taken on each of the smooth and rough boundary tests in the large flume were those required to calculate the following quantities: the hydraulic radius, the Reynolds number, the Froude number, the Darcy-Weisbach friction factor, the channel opening ratio M^0 , the discharge coefficient, the backwater ratio (y_1/y_n) , the backwater superelevation $(h^*_{\ 1})$, the surface profile ratio $(h^*_{\ 1}/\Delta h)$, the length to the maximum backwater (L_{1-2}) , the length to the point of minimum depth (L_{2-3}) , the length L_{1-3} , and Manning's n. (See Figure 1 for the definition of terms). In view of the large amount of data that was to be analyzed and the repetitive character of the calculations, a program was prepared for processing the data on the Royal McBee LGP-30 digital computer.

The tabulation of the test data may be found in reference (17)**.

ANALYSIS OF TEST RESULTS

Large Flume Smooth Boundary Model Tests

The experimental results of the two dimensional, semicircular, arch model tests in the large flume with smooth boundaries were plotted

A copy has been deposited at the Engineering Societies Libraries.

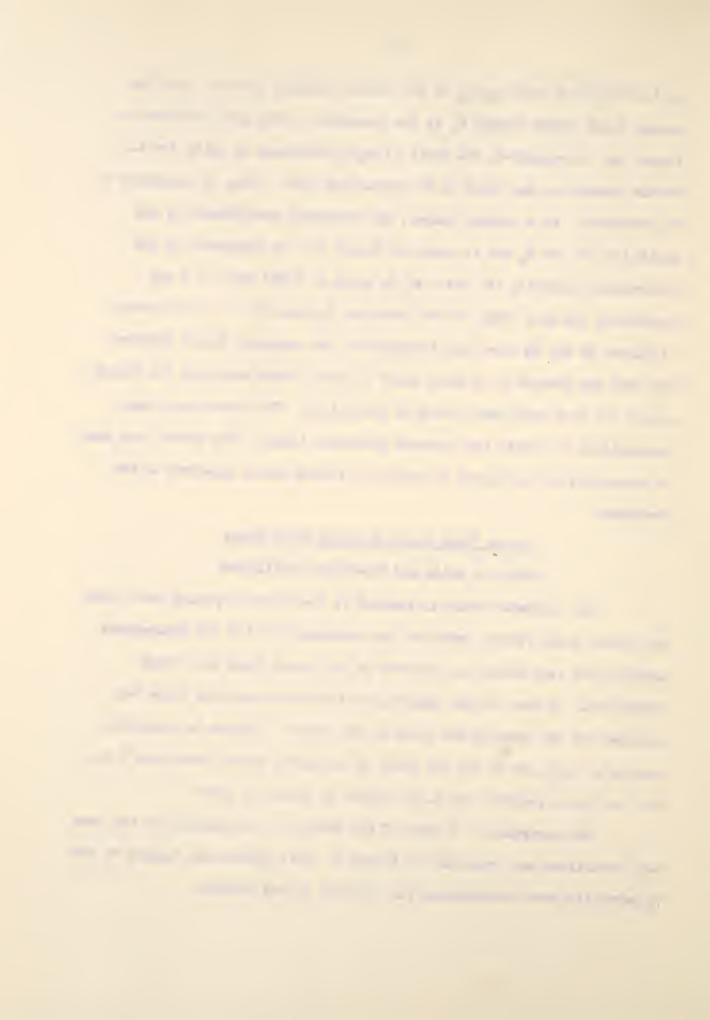


normal depth Frond number F_n as the parameter. This plot is shown in Figure 6a. As expected, the ratio of y_1/y_n decreased to unity for all. Fronds numbers in the value of Mi approached 1,00. Also, it increases as Mi decreases. In a similar manner, the discharge coefficient C_d was plotted vs Mi for F_n and is shown in Figure 6B. As discussed in the theoretical analysis, the value of C_d tends to 0.611 at Mi = 0 and approached the sum value at the parameter F_n was $M^0 = 1$. The curves of Figure 6a and 6b have been interpolated for constant fronds numbers. This data was plotted on a large hier of graph paper such that the Fronds curber for each data point could be identified. The points were then interpolated to obtain the curves in with the Fronds number appeared as the parameter.

Large Flat 1 on toundary Model Testa Backgater datio and Discharge Coefficient

The backwaier ratio is plotted vs the channel opening ratio with the normal depth Fronce number at the parameter for the two dimensional semicircular arch models as observed in the large flux with rough boundaries. In view of the importance of those curves, the scale was expanded and the results are shown in two parts. Figure 7a gives the results of $y_1/y_1 = 0$ for the range of backwater ratios less than 1.50. For the ratios greater than 1.50, Figure 7b should be used.

The experimental values of the discharge coefficient for the same test conditions are presented in Figure 8. This figure and Figures 7a and 7b have also been interpolated for constant Froude numbers.



Loc 1 3 Pois of I within Bac atar, and Mi immo Dapila

In or to ces with the conterling profile it is desirable to have an astama. The listance orem the postreat face of the constrict tion . The till f max or backen or ale tion. This dictance is referred to an 19.2. Breat of the Claimese of the strings profile in the vicinity of the rattern sent, it we are marky difficult to get in exact measures ment of the actual sweet its taken could have been in orrow by as much to the term . Here there we see the large amount of data which was while do it to a result to the Light of an average busis. Average values of 12 ste calculations of b/B, L/b, L/D, etc. In manner it appered that the effect of the variable oridge ler in all he chan in a percoff the same order to magnitude as the experiment error for most consistent relationship was found by plotting the dimensionless ratio in .2/6 we the Froude member F, with M = b/B as the at latera and is not the nichip is shown in Figure 9a. The values of a phtaine of one a smooth boundary tests also compared ferorable the light of see that he remove it was found that the length by a (d. t. see from the rath an depth point to the minimum depth points, seried may with the communication geometry, The values of Lieg/b are plotted ve 1 - e/3 with 1, and parameter in Figure 90. These curves are good for onth ore and three dim national samistroular arch bridges.

beterministed of the liniage Depth

Save I there investigates have used the Fronds number at section 3 (F3 = V_3 / \sqrt{s} F3, as a controlling parameter in making indirect measurements of flood discharges. Due to the extremely irregular flow pattern at the minimum of the it would be like the use of F3 may be misleading.

In the process a week, we have the largest in making indirect measurements of flood discharges. Due to the extremely irregular flow pattern at the minimum of the it would be like the use of F3 may be misleading.



a very reliable estimator of $\mathcal{F}_1/\mathcal{F}_1$. In order to test the wriability of F_3 with F_{15} , a correlation curve of F_3/F_1 v. F_1 was prepared. This curve is shown in Figure 10. Below a Froude number F_7 of 0.5, the correlation was good. However, about $F_1=0.5$, the depth y_3 was often below the critical depth and the correlation of F_3/F_1 t. F_1 was very poor. The scatter seemed to increase with increasing values of F_3/F_2 t. Therefore only the test results of the F_3/F_2 to the are them. If F_3/F_3 depth F_3/F_4 the properties of the F_3/F_4 to F_3/F_4 the minimal depth F_3/F_4 . It appears from this curve that F_3/F_4 is such note reliable parameter than F_3/F_4 .

Comparison of Roughness Effects

Comparisons between the model tests in the emooth and rough channel were reds by plotting the tackwaiser retio and the discharge coefficient again t the normal depth Fronds number F_n for constant channel opening radios.

It appeared that the values are ersentially the same for both smooth and rough conditions at Freedo numbers Fn less than 0.5. Since the practical range of fixedo numbers for natural channels is that less than 0.5, these curves should be all practical purposes the effect of roughness can be ignored.

Comparison of Bridge Length Effects

Similarly, all of the L/s results were compared at constant values of the channel opening ratio M° . Again it appears from the plots for that/the practical range of field conditions, (L/s \leq 1.0 and $F_{\rm R} \leq$ 0.5) the effect of bridge length in regligible. The effect of length did seem to increase with a decrease in the channel opening ratio. However, as the value of M° gets small, the physical properties are closer to those of a culvert rather than a bridge opening.

The second secon

The second of the diagrams is given due to the second of the diagrams is given due to the second of the diagrams is given due to the second of the diagrams is given due to the second of the diagrams is given due to the second of the diagrams is given due to the second of the diagrams is given due to the d



checked that measured with the verturi met p nithin 1%-

In addition is over diagrams were obtained for the other uniform flow condition. From the diagrams and from Figure 12a, the following values of the kinetic energy correction factor and the momentum correction factor. The obtained for uniform flow or dillions:

Q	Slope	y ₁₂	App ce n	a	ş
2 of	C 000131	0.799 210	0.10	10145	2 055
1 cfs	0.0287	0.319 fts	U=21	1 216	1.084
l eff	7 004080	0 ur3 Et	0.53	L. 250	2 090

Based upon a conversion of a locally profile for Q = 3.71% of and S=0.0125

the value of c. was determined at 1.01. This alue, based on an assumed

two dimensional flow, is less than that of 1.145, 1.216 and 1.250 d termined

from the integration of the isovol diagram which took into account the

effects of the sides and corner. Other investigators have assumed that

oxis unity for a rigid rectangular flume. This calculation verifies that

this assumption I correct if the flow is nearly two dimensional.

THE GETERALIZE BACKVATER EQUATION

With the introduction of the channel opening ratio M, to account the barreter produced by constrictions of the same M, would be equal regardless of the physical geometry of the actual constriction. In order to verify this assumption, test data on constriction geometries other than a semicircle was needed.

A series of 95 tests were run by A. A. Sooky in the small flume on two dimensional segment weirs with a $\eta = d/r$ value of 0.5. (see Figure 2). The data obtained were analyzed in terms of M'. These tests were run in the small channel with rough boundaries which had a Manning's n of 0.000. Re lits were plotted in the same manner as for the large flume

rough to to and are shown in Figur 13. When compared to the large Thurse results of Figure ", the values of the backwat r ratio for a given by and M' are almost denti- Inspire of the fact that each set of curves had been interpola ed, the small disferences could easily be attributed to experimental an graphical error.

In a limiter man r, the vertical board date given by Liub was resnally and to fit the yy/y . In the dof presentation. These tests were run in a libration with thisfer to arghness pattern. Their roughness would a Manning on of 0.00%. The results were compared to the oni-circular date given previously and to the beginst data. Again the differences were entremely and I and at tributed to experimental error. It is entremely interesting to note that he test data taken by three investigators in three different flums and under three completely different constriction geometries produced almost identical results. This clearly verifies that the channel opening ratio M is a governing variables. Of course, the data compared here those in which the countricity was zero, the akes was zero, and the entrance was sharp.

should be a common relationship between the backwater ratio y_1/y_n , the frouds number F_n and the channel opening ratio H^* which would fit all of the data. This relationship should then be applicable to all constriction geometries. As rentianed previously in the tralysis, a similarity was noticed between the several different backwater equations. The term $(F_n/H^*)^{2/3}$ appeared in all of the solutions of y_1/y_n . In general, it appeared that

$$J_1/J_n = C \left[(P_n/M^2)^{2/3} \right]^{2}$$
 -- (28)

- 1 - 1 - 1

where C is a finish. At the world all into constant the effects of the discharge of finish. The average is finish. The average is relative to the constant and the constant and other are relative to the finish of the constant and the constant and the constant and the constant are also beard value. Colorado and the constant are also beard value. Colorado and the constant are also the constant and the constant are also beard value. Colorado and the constant are also the backwater at the constant are also be constant as a constant are also be constant as a constant are a constant as a constant are also be constant as a constant are a constant.

The mathed of lists spread applied to a nunder sample of the 15% and points to determine the expired straight line relation hip.

After solving is a and C, equality (5) because

produced by any time of continuous. In ctual practice, this equition for the bankwater migrated thid.

It has been suggested by C. F. Izzard that equation (29) could be approxumated by

$$y_1/y_n = 1 + 0.45 (1 / M^3)^2$$
 --- (30)
and still fit the Jata vary closery.



HODEL PROTOTYPES COMPANISON AND LASTON PROCEDURES

The most apportant variables in de semining the meximum backwater are the normal depth Frond made In and the homest of Mich.

As defined, Mich be used for my type of bridge generative. The boundary roughness and the bridge lar th for Fronds in are less than 0.5 are relatively united and in the first of all practical purposes, and se neglected in malyzing the first of the first difficulty cometime arizes in defining the normal depth at the normal depth for an irregular result hannel. The could be the Fronds number for an irregular matural channel. We not a hydraulic depth of yn should be taken a An/En, when An In the united a file cross at foral area and En is the uniform file, so the width. The Froude in ber is defined as

$$P_n = \frac{1}{2} / \sqrt{8} y_n / \alpha = \sqrt{(q^2 + 1/4^3 g)} / \alpha = \sqrt{31}$$

For the 1 reduces ...

$$r_{\rm B} = r_{\rm c} / \sqrt{\epsilon r_{\rm c}}$$
 $\sqrt{2^2 r_{\rm b} / r_{\rm b}^2} \epsilon$ $\sim (32)$

The office of the linetic correction factor of on the Fronds number, may the evaluate from the placity distribution. It is customarily assumed that the incorporation of the ideatic energy correction factor of into the field calculations would account for a partion of the differences between moduland prototype. This can be done in the following way. For similarity it is necessary that

(
$$\forall \sqrt{g} y_n / \infty$$
) model = $(\sqrt{q^2} E_n / A_n^3 g / \infty)$ prototype
($\forall \sqrt{g} y_n$) model = $(\sqrt{q^2} E_n / A_n^3 g)$ protytype $\sqrt{(O_p/N_n)}$ —(33)

The second secon

The second second

A AMERICAN CANADA

the state of the s

THE RESERVE OF THE PARTY OF THE

The same of the sa

When α_p is approximately quality α_m the effect of the kinetic energy coefficient may be neglected. In actual natural stream it is of the order of 1.25 which is very class to the present experimental values. In what follows, the ratio of (α_m/α_m) as taken a unity. However, its effect could be evalued by mach of equation (33).

Birtiga nututana

The bolt experimental approximation to the backwater ratio for semicircular and bridges ultimate some eccentricity or intrance rounding is given by figures hand 7b. Equation (23) and do used to calculate yellow by obtaining the discharge coefficient from Figure 6. A more practical first approximation to the maximum ackesser is given by the curves of Figure 1; or by a without (29) or (30).

In the one of the state of the same

If the concepts present d in while paper are und as a method for making indirect estimations of flood discharges, the following detailed procedure is recommended. The state outlined provide an estimation and not a direct calculation.

A. Freliminary Compute ions

- 1.) Obtain from a field survey a cross-section view of the stream at the approach section (section at the maximum backwater slevation) and at the upriream face of the bridge.
- 1.) For several elevations determine the area below that
 elevation for e.ch section. This is most readily
 accomplished by plotting the section views to a
 fairly large scale and using an area planimeter to obtain
 the respective areas. Also for each elevation, determine
 the surface widths at the approach section.

The same of the sa and the same of th

- 3.) With the respective elevations, area, and surface midths plot the four working our is shown in Figure 15.
- P. Trial and Erro. Solution for the Dischar
 - 1.) From the sure of high word, marks, obtain the meximum surface elevature for the given flood.
 - 2.) Fater cur (3) fish this il veticn and obtain the maximum grafe a viden B. (max.)
 - 3.) With 3; (= u) out rous (') and obtain y; (max.)
 - 40) Assume a value of the normal hudraulic depth yn(yn yl).
 - 5.) Lith yr. A/B get the asset d normal depth surface width

 From cur. (;).
 - 6.) Enter cure (3) with Bul and obrain the corresponding levelier.
 - 7.) With this elevation obtain the value of the channel opening retio M* Ang/Ang and the nursel depth approach area Ang from our at (2) and (1) respectively.
 - 2.) Compute y_1/y_n and obtain the normal depth Froude number from equation (29).
 - 9.) With the Fronds number Fn defined as equation (32), calculate the discharge Q. This will give a first estimate of the flood discharge:
 - 10.) With M⁰ and F_{F1} go to Figure 8 and obtain the discharge coefficient C₆.
 - 11.) As a second estimate, compute the discharge according to equation (15), where b is the distance between abutments at the epringlish of the arch, i is the radius of curvature of the arch, i is the radius of curvature.

the second of th The second secon THE RESERVE TO SERVE THE PARTY OF THE PARTY

Lurfac Intuition to the wireg bott. at the inidge section in wireg to the dipth is computed in the retion. I do not be and to the library in the retion of the arch to the library in the retion.

12. I'm dieg of he me a comprise by resp ? of

B i. . I'm the man completed If they are not

publication of the median in public the

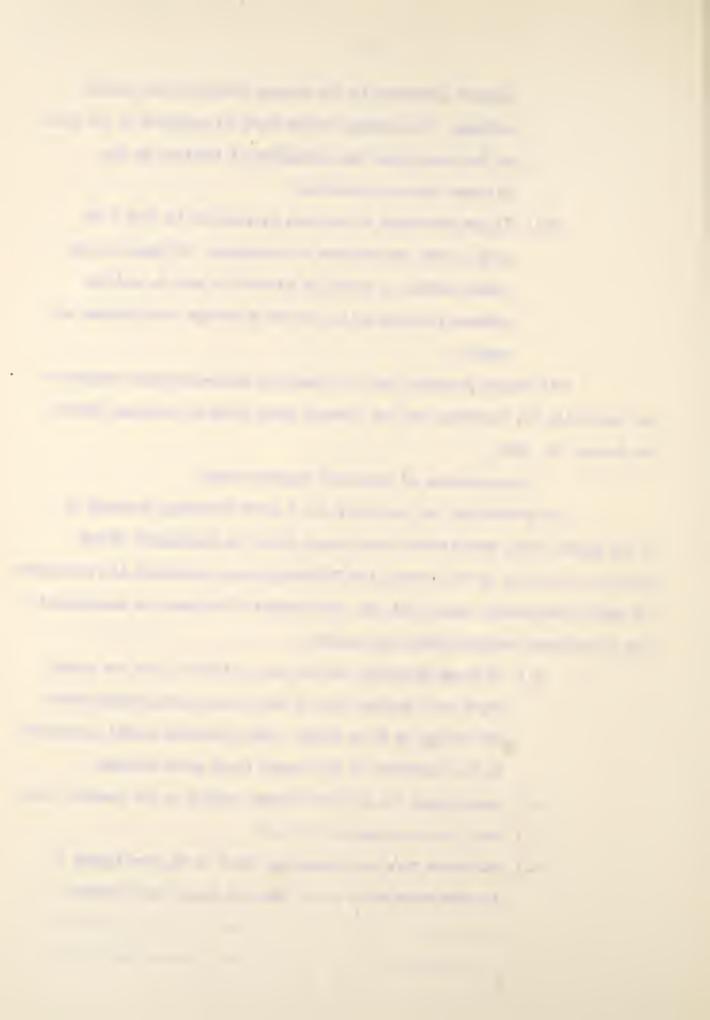
process. In all internations discharge calculations are

The second of th

la resident of la distance of produce the

The state of the s

- left of a control of the stream ross-section where
 the bridge to built. This elevation should correspond
 to the all vettles of the design flood water surface.
- 2.) Sup ring a the proposed bridge profile on the section view.
- 3.) Determine the vilue of M = b/B.
- 4.) Calculate yn/r and obtain the value of CM from figure 5 for the curve of 7 = 0. When the center of curvature



- : below to pringline of the arch, shoulate d/r and the distribution of the arch, shoulate d/r and the obtain C_{M°
- 5) Calculate in my loopel. Frude number Fallon equation (32).
- 6. Orlegist 1 1 1
- 7.) Ith M and A the rate of y_1/y_1 is a sither . In appear to value can also be the time $x_1 = x_2 = x_3 = x_4$. It is equation (29).
- the Factor of Land Alagan postively.
- 9. Larond with a of the Limm depth is desired,

 Equate 10 can be applyed:

 Frankly 1. 1 of Fourted by the Area

the design of the days such that is a sultang real in backater will not use a cost to the first product a such a supertant when severe as creather of the first plant is note. It is design flood discharge is available, the corresponding dains brought through the sway area can be allowed. The following promotion is returned.

- lo) On a vi w of the errorm of mes-section, plot the normal lags election for the design flood.
- 2.) Calculate the elevation of the hydraulic bottom. (W.S. lev. normal hydraulic topy) at section 1.)
- 3.) Calculate the ta keater raid yl/yhwhere yl is the hydraulic depth corresponding to the given permissible maximum water surface.
- he (otain and Bar from this section view for the maximum



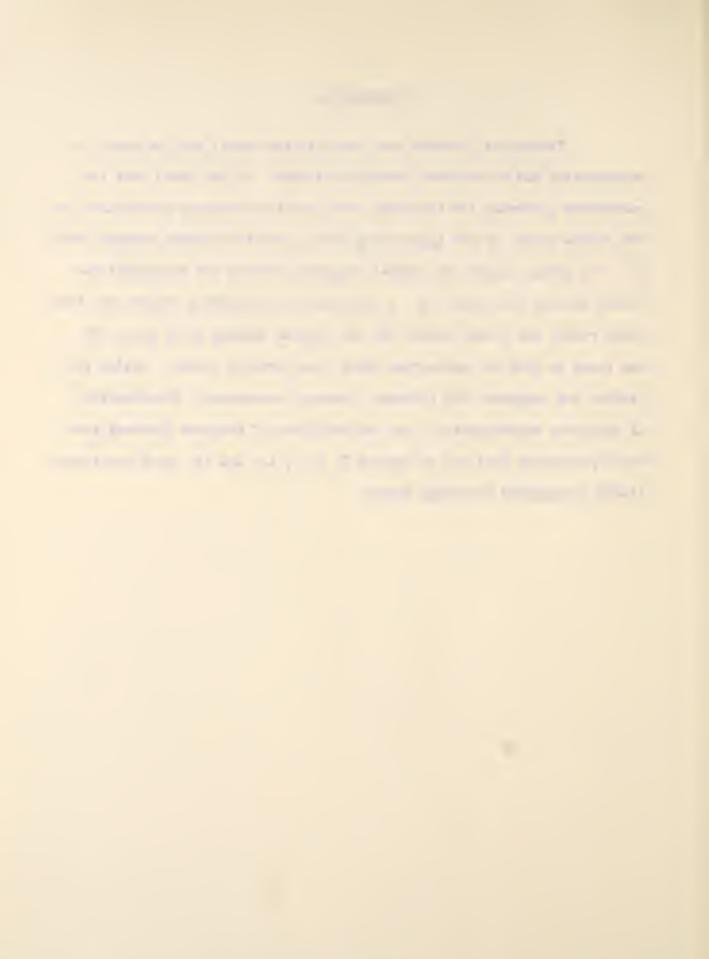
- 5.) Lith y_1/T_1 and F_n calculate the channel opening ratio from equation (29).
- 6.) With M' and And compute the required minimum normal depth are no s Ang = 10 Ang.
- 7.) Adjust the upon a dth, radius of curvature and the depth to the call r or arvature to fit the required ministra area Ang

Crooked the k Hood of J no w 21, 1950 at Madison, Indiana

The model-protetype temp rison is done according to the design procedure returned for anti-wing flood discharges at each bridge constrictions. The field will y data is part of a report on the indirect estimation of gloods by the office of the U. S. Geological Survey in Indianapolis, Indiana. The flood under study is one that occurred on January 21, 1959 in the Crocked Green at Midison, Indiana. Following the procedure which was outlined by Mindevster, Carter and Tracy in reference 5, the Survey estimated the flood to be 4200 offe. Although the arch is essentially semicicular and without above, the rather high degree of eccentricity and the extremely irregular channel section makes the present system of surly is somewhat doubtful. The value of the discharge obtained by the proposed method are 4560 after or about 2% larger than that calculated by the U.S.G.S.

CONCLUSIONS

coentricity and no entermore rounding was made. It was found that the parameters governing the boundth of ratio and the discharge coefficient are the Fronds number of the procedure effects are negligible for Fronds number less than 0.5. A generalized relationship between the backwater ratio, the Fronds number of the add the channel opening ratio (equ. 29) was found to hold for geometries other than directlar arches. Design procedures are suggested for indirect discharge measurement, determination of backwater superclevals, and determination of required waterway area. These procedures make use of figures 7, 8, 9, 10, and 14, which are tentatively recommended as design curves.



ACK NOWLEDGMENT

This research was sponsored by the State Highway Department of Indiana in cooperation with the U S. Department of Commerce, Bureau of Public Roads. The authors wish to express their appreciation to Mr C. F. Izzard, Director of Hydraulic Research, U. S. Bureau of Public Roads, Washington, D. C., for his valuable comments and suggestions and to Mr. H. J. Owen, Associate Research Scientist, Illinois Water Resources Commission, Urbane, Illinois, the, while a Research Assistant at Purdue University, designed and supervised the construction of the large flume and started the model testing with smooth our darks. Thanks are also given to Mr. A. Social, Research Assistant at Purdue University, who performed the testing of segment arch models in the small flume

BIBI TOGRAPHY

- lane, E. W "Experiments on the Flow of Vater Through Contractions in Open Channels", Trans. ABCE Vol. 83, 1910-20 pp 1149-1219
- Kindevater, C. E. and Carter, R. W. "Tranquil Flow Through Open-Channel Constructions", Trans. ASCE, Vol. 120, 1955, pp. 955-980.
- 3. Tracy, H J. and Carth, R. W. "Backwater Effects of Open-Channel Constrictions", Trans ASCE, Vol. 120, 1955, pp. 993-1006.
- 4. Izzard, C. F. Discuss ons on "Rackwater Effects of Open-Channel Constrictions" by H. J. Tracy and R. W. Carter, Trans. ASCE, Vol. 120, 1955, pp. 1003-1013.
- 5. Kindsvater, C. E., Carter, R. V. and Tracy, H. J. "Computation of Peak Discharge at Constrictions", U.S.G.S. Cir. #284, Washington, D. C., 1953.
- 6. Liu, H. K., Bradley, J. N. and Plate, E. J. "Backwater Effects of Piers and Aburments", Colorado State University, CER57HKLIO, October, 1957.
- 7 Bradley, J. N "Hydraulics of Bridge Waterways", U. S. Department of Commerce, Bureau of Public Roads, Washington, D. C., August 1960.
- 8. Vallentine, H. R. "Flow in Rectangular Channels with Lateral Constriction Plates", La Houille Flanche, Jan. Feb. 1958, pp. 75-64.
- 9. Herbich, J. B., Carle, R. J. and Kable, J. C. "The Effects of Spur Dikes on Flood Flow: Through Highway Bridge Constrictions", Fritz Engineering Laboratory, Lahigh University, June, 1959.
- 10. Owen, H. J., Socky, A. A., Husein, S. T., and Delleur, J. W. "Hydraulics of River Flow Under Arch Bridges A Progress Report", Proceedings of the 45th Road School, Purdue Engineering Experiment Station, Series No. 100, March 1960.
- 11. Buckingham, E. "On Physically Similar Systems", Phys. Rev., Vol. 4, Ser. 2, pp. 345-376, 1931
- 12. Streeter, V. L. "Fluid Dynamics", McGraw-Hill Book Co., New York, 1948, pp. 174-177.
- 13. Owen, H. J. "Design and Construction of a Hydraulic Testing Flume and Backwater Effects of Semicircular Constructions in a Smooth Rectangular Channel", Progress Report No. 2, Joint Highway Research Project, Purdue University, January, 1960.
- 14. Daugherty, R. L. and Ingersoll, A. C. "Fluid Mechanics", McGraw-Hill Book Co., New York, 1954.

-51 -711 "

The second secon

- 15. Chow, V T "Open Channel Hydraulics", McGraw-Hill Book Co., New York, 1959.
- 16. Henry, H. F. Piscussion on 'Diffusion of Submerged Jets", by Albertson, Pai, Jensen, and Douse, Trans. ASCE, Vol. 115, 1950, pp. 687-694.
- 17. Biery, P. F. and Delleur, J. 1. "Hydraulics of Single Span Arch Bridge Constrictions", Report No. 5, Joint Highrey Research Project No. 0-36-623 cottol of Civil Figureering, Purdue University, Lafayette, Indiana.



NCTATIONS

SYMBOL	UNI PS	
A	Lk	Aves
Anl	L	Total normal depth flow area at section 1
A _{n2}	13	Normal depth flow area at section 2
8	L	Roughness height
В	7	Recta gular channel width or surface width for a non-rectangular channel
ь	I,	Span width at the springline of the arch
C		A coefficient
С	I) '/T	The Chery roughness coefficient $\sim V_{\rm h}/\sqrt{R_{\rm h}S}$
c _d		Cooff clent of discharge
Cef		Channel opening ratio coefficient
D	7.	Hydraulic depth as defined by V. T. Chow
d	L	Dapth of flow in a steep open channel
Ġ	L	Distance from the springline to the center of curvature of the arch
¥**		Denotes a mathematical function
r _n		Normal depth Fronce number = Vn/ VEVn
F3		Froude number at the section of minimum depth
Í		Denotes a mathematical function
£		Darcy-Weisbach friction factor
G		Denotes a mathematical function
8		Denotes a mathematical function
g	L/T ²	Acceleration of gravity
H	Ĭ.	Total energy head

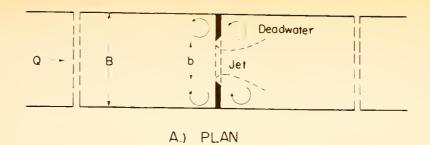


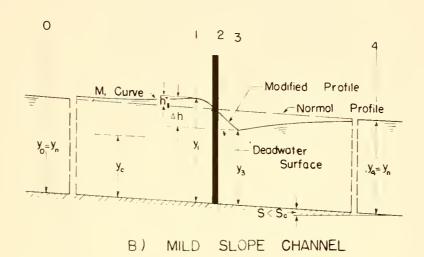
h	L	Barkwater superelevation
h	L	Difference between the maximum and minimum surface elevations
i		Subscript denoting a subsection of an isovel dirr
Ж		Vol. coefficient
		a constant to the correct
L	L	Langta of the bridge parallel to the direction of the flow
11-2	L	The distance along the centerline from the versam face of the bridge to the maximum because election
^L 2-3	Ĺ	The stance elements the conterline from the upper am face of the bridge to the minimum say, the elevation
М		Chann I width ratio b/s
M		Chain 1 opening ratio
M		Mile lope backwater curve in an open channel
n	L'/6	None ingle roughness coefficient
n		Subscript which r fors to the normal depth for uniform flow
p	F/L ³	P-c 12 18
Q	L ³ /T	Total flow
q	L ³ /T	That fortion of the total flow which could pass through the bridge without contraction
R	I	Hydra Lic radius
Σ°	L	Radius of curvature of the arch
S		Slope
Ţ		An infinite series of powers of the ratio of the maximum depth to the radius of curvature



v	L/T	Average velocity
v	I./T	local velocity
F	L	Depih of flow
yn	L	Depth of the normal unconstricted flow
y	L	Depth of flow at the section of maximum backwater
y ₂	L	Depth of flow at the vena contracta
¥3	L	Minimum depth of flow
d		Kinetic energy coefficient
β		Momentum coefficient
8	F/13	Specific weight of water
3		Ratio of y _n / r
3		Retio of d / r
7	L ² /T	Kinematic viscosity of the fluid
e	FT ² /L ⁴	Fluid mass density







C.) WEIR PLATES

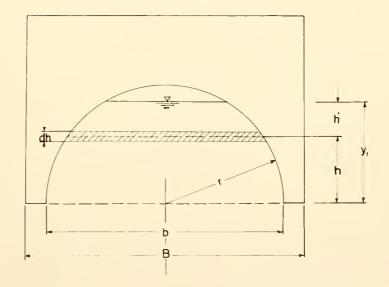
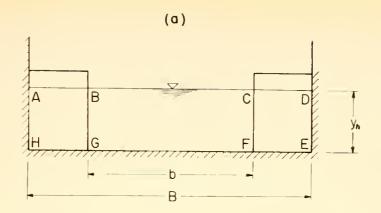


FIGURE | DEFINITION SKETCH





FLOW IN ADEH = Q = Vn Byn

FLOW IN BCFG = q = Vabya

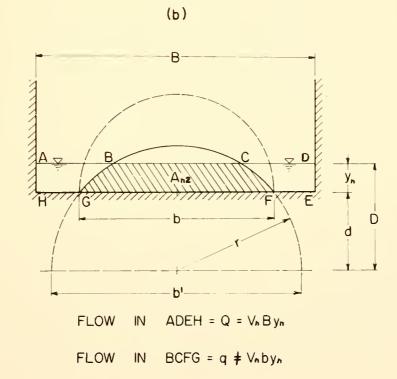


FIGURE 2 - DEFINITION SKETCH FOR THE DEVELOPMENT OF

THE CHANNEL OPENING RATIO



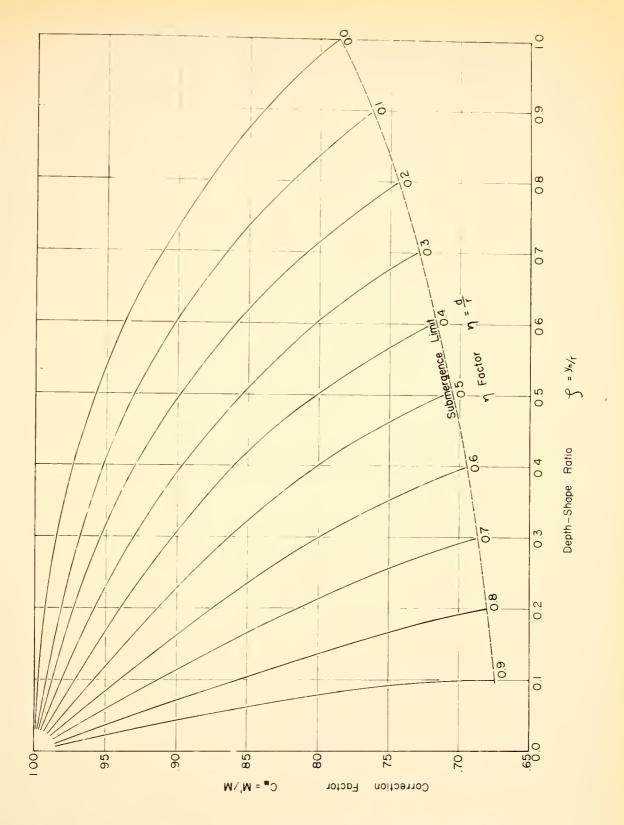


FIGURE 3 — CORRECTION COEFFICIENT FOR THE CHANNEL OPENING RATIO



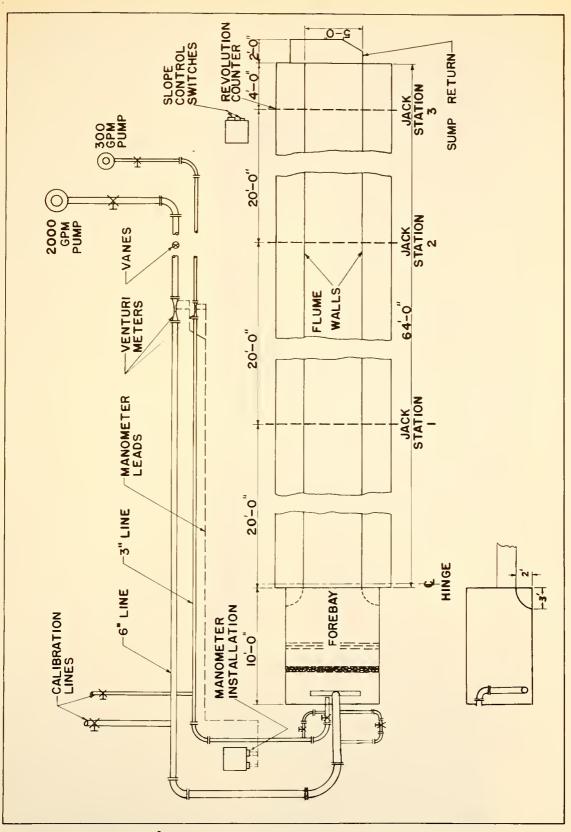


FIGURE 4 - APPARATUS ARRANGEMENT



FIG 5 MODELS



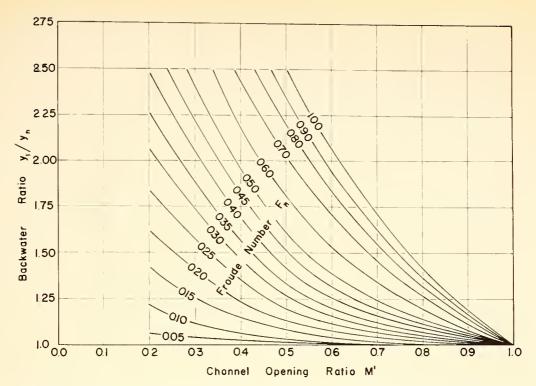


FIGURE 60 — BACKWATER RATIO VS CHANNEL OPENING RATIO L/b=0 SEMI-CIRC. SMOOTH CHANNEL

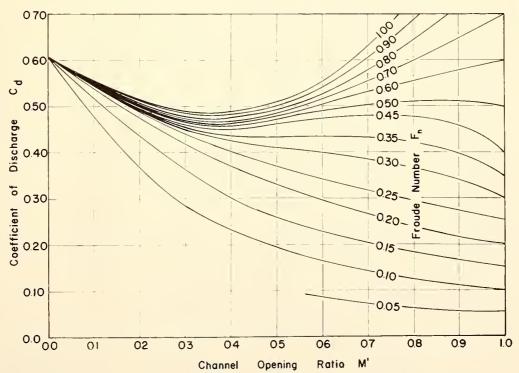


FIGURE 6 b — DISCHARGE COEF. VS CHANNEL OPENING

RATIO L/b = O SEMI-CIRC SMOOTH CHANNEL



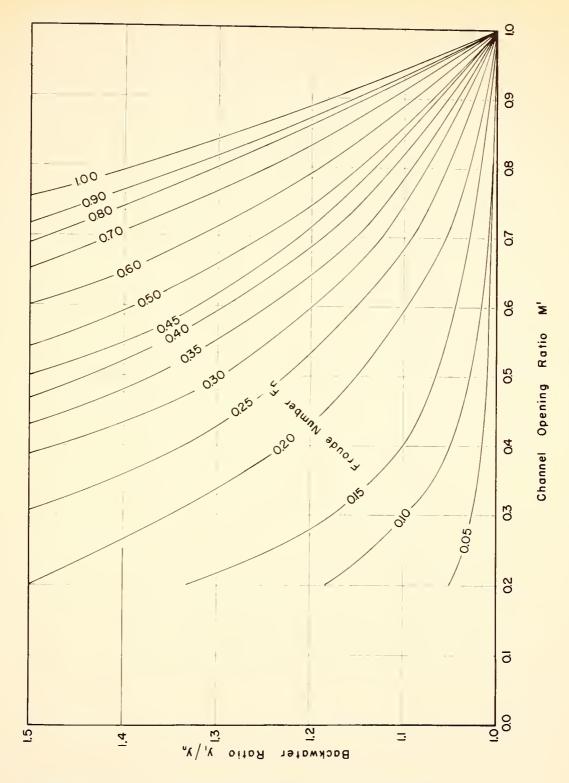


FIGURE 70 — BACKWATER RATIO VS CHANNEL OPENING RATIO L/b=0 SEMI-CIRC. ROUGH CHANNEL $y_{_{\rm I}}/y_{_{\rm R}} \leqslant 1.50$



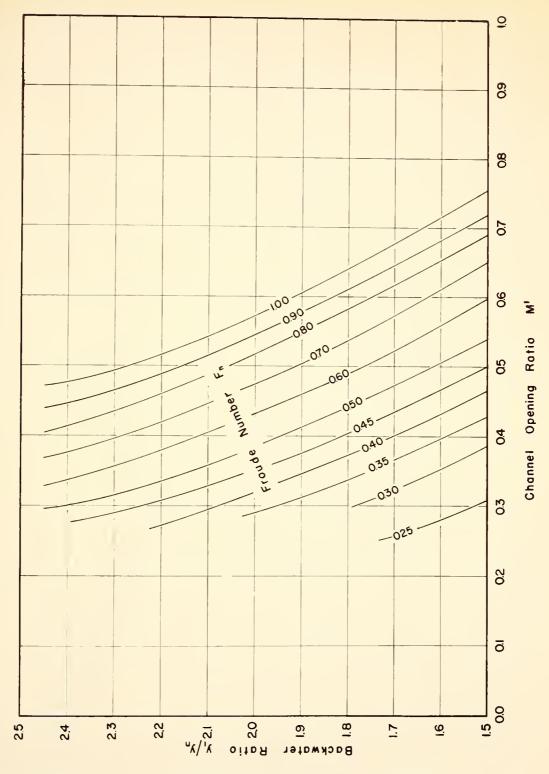


FIGURE 7b — BACKWATER RATIO VS CHANNEL OPENING RATIO L/b=0 SEMI-CIRC. ROUGH CHANNEL 1.50 \leq $y_i/y_n \leq$ 2.50



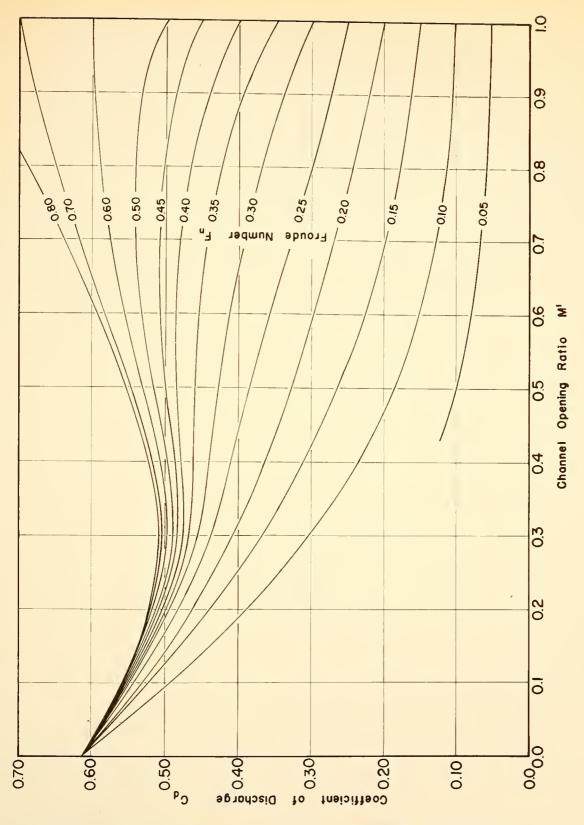


FIGURE 8 -- DISCHARGE COEF. VS CHANNEL OPENING RATIO L/b=0 SEMI-CIRC. ROUGH CHANNEL



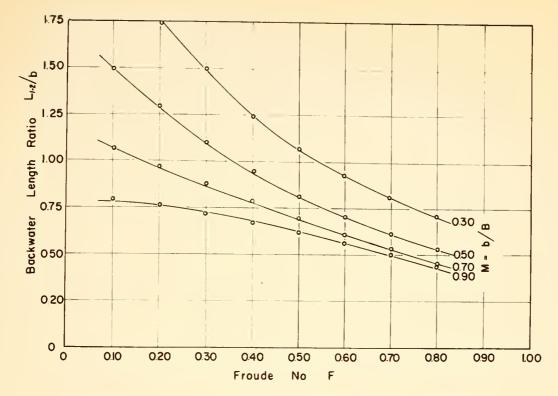


FIGURE 9 a - LENGTH TO MAXIMUM BACKWATER

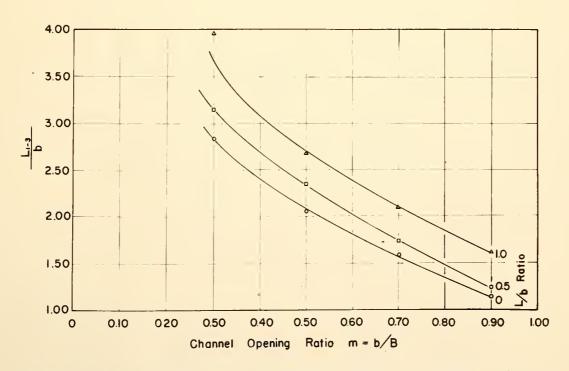
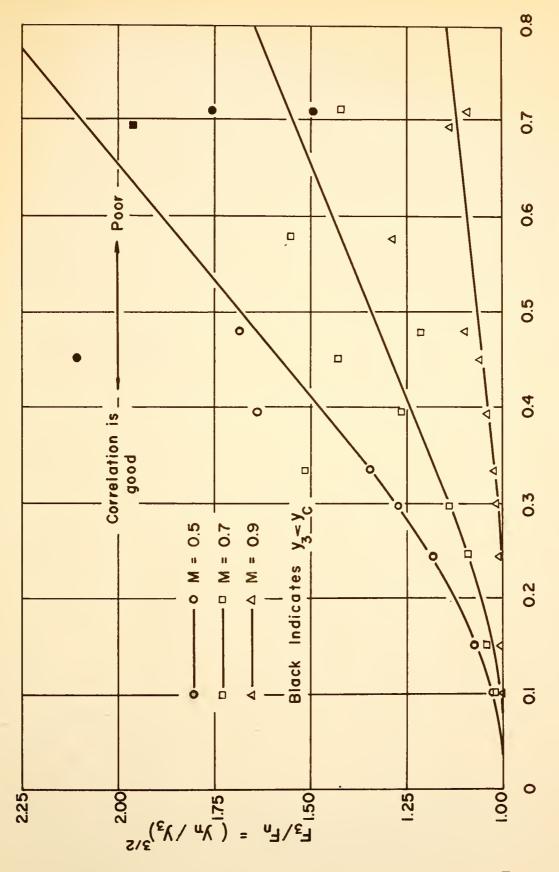


FIGURE 96 - LENGTH OF SURFACE PROFILE BETWEEN 1, 4 1,





u.c

NORMAL DEPTH FROUDE NUMBER

FIGURE 10 - CORRELATION CURVE OF F3



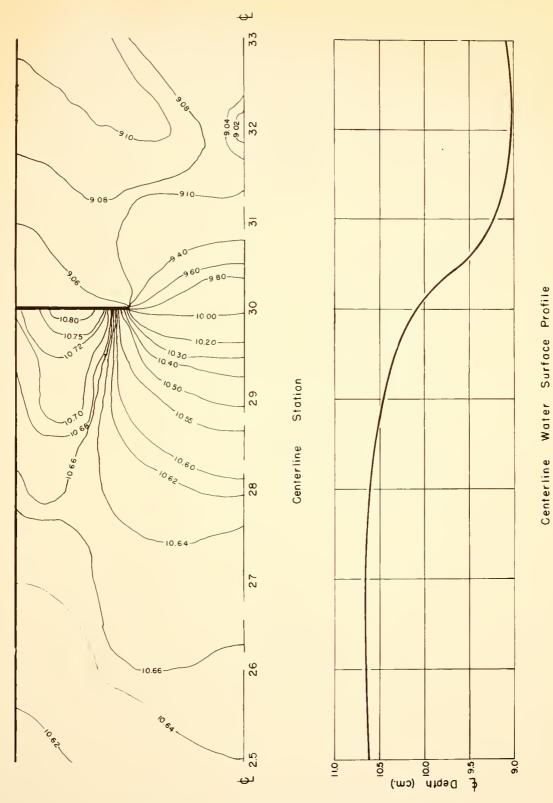
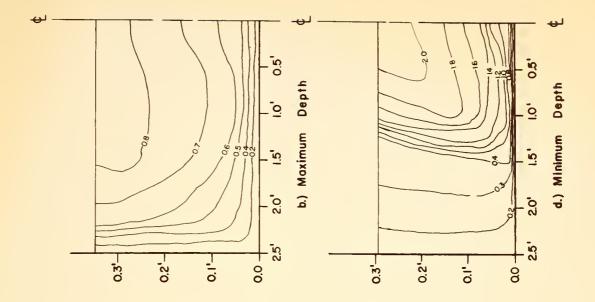


FIGURE II - SURFACE TOPOGRAPHY Q = 1 cfs, S=0.000584, M=0.5, L/b=0





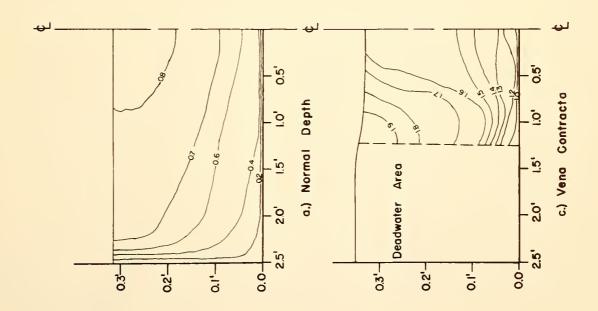


FIGURE 12 -ISOVEL DIAGRAMS IN FPS Q=ICFS, S=0.000584, M=0.5, L/b=0



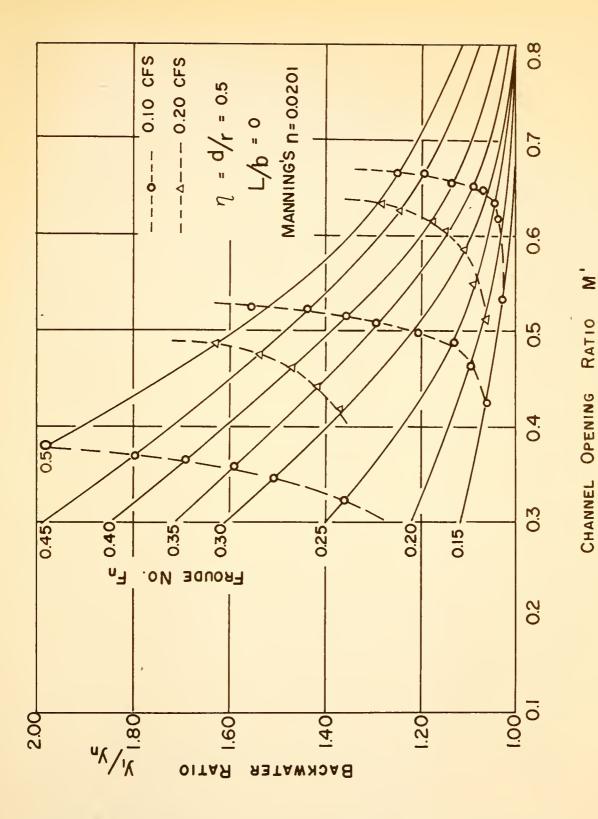


FIGURE 13- VARIATION OF THE BACKWATER RATIO FOR SEGMENT ARCHES SMALL FLUME - ROUGH BOUNDARIES



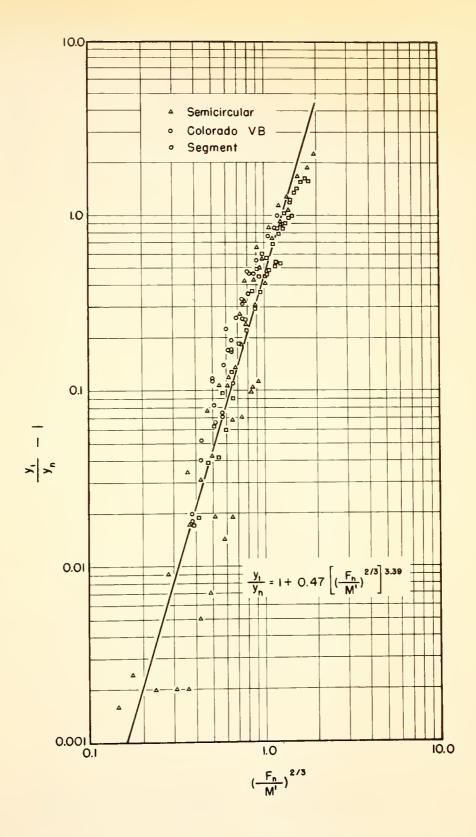


FIGURE 14 - GENERALIZED BACKWATER RATIO



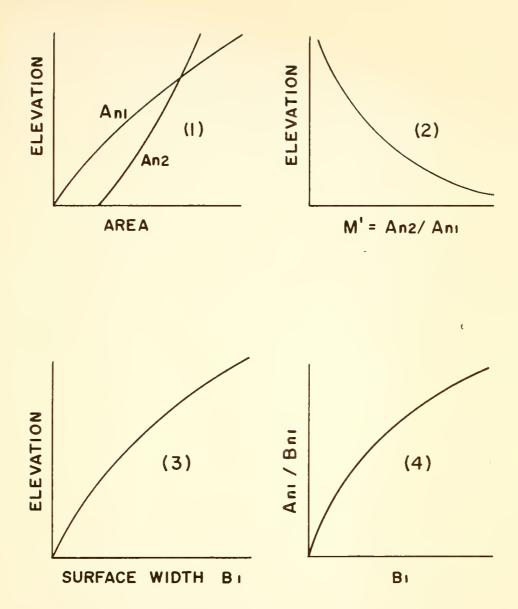


FIGURE 15 - WORKING CURVES FOR INDIRECT DISCHARGE MEASUREMENT





